



B.Tech - Odd Sem : End Semester Exam
Academic Year:2020-2021
19CS2104 - Mathematical Programming-1
Set No: 1

Time:		Max.Marks: 100																													
S.NO	Answer All Questions	Choice	Options	Marks	CO																										
1.	A hotel has requested a manufacturer to produce pillows and blankets for their room service. For materials, the manufacturer has 750 m ² of cotton textile and 1,000 m ² of silk. Every pillow needs 2 m ² of cotton and 1 m ² of silk. Every blanket need 2 m ² of cotton and 5 m ² of silk. The price of the pillow is fixed at \$5 and the blanket is fixed at \$10. Formulate the problem using mathematical modeling of LPP and define the objective function. What is the number of pillows and blankets that the manufacturer must give to the hotel so that these items obtain a maximum sale?	choice Q-2		10Marks	CO1																										
2.	<p>The tactical border bomber squadron receives orders to disrupt the rival tank fabrication. In different towns the opponent has four major plants, if any one of the plant is destructed then the production come to halt. The fuel available for the mission is only 45,000 liters. In the least, a bomber flies to a specific city should have a minimum fuel enough for a complete round trip and an additional 100 liters of fuel is required. To optimise the likelihood of success, how many of each type of bombers should be dispatched, and howshould they be distributed among the four targets?Formulate the linear Programming.</p> <p>The number of bombers available to the commander and their descriptions, are as follows:</p> <table border="1"> <thead> <tr> <th>Bomber type</th> <th>Description</th> <th>Km/litre</th> <th>Number available</th> </tr> </thead> <tbody> <tr> <td>A</td> <td>Heavy</td> <td>2</td> <td>40</td> </tr> <tr> <td>B</td> <td>Medium</td> <td>2.5</td> <td>30</td> </tr> </tbody> </table> <p>Information about the location of the plants and their probability of being attacked by a medium bomber and a heavy bomber is given below:</p> <table border="1"> <thead> <tr> <th rowspan="2">Plant</th> <th rowspan="2">Distance from base (km)</th> <th colspan="2">Probability of destruction by</th> </tr> <tr> <th>A heavy bomber</th> <th>A medium bomber</th> </tr> </thead> <tbody> <tr> <td>A</td> <td>Heavy</td> <td>2</td> <td>40</td> </tr> <tr> <td>B</td> <td>Medium</td> <td>2.5</td> <td>30</td> </tr> </tbody> </table>	Bomber type	Description	Km/litre	Number available	A	Heavy	2	40	B	Medium	2.5	30	Plant	Distance from base (km)	Probability of destruction by		A heavy bomber	A medium bomber	A	Heavy	2	40	B	Medium	2.5	30			10Marks	CO1
Bomber type	Description	Km/litre	Number available																												
A	Heavy	2	40																												
B	Medium	2.5	30																												
Plant	Distance from base (km)	Probability of destruction by																													
		A heavy bomber	A medium bomber																												
A	Heavy	2	40																												
B	Medium	2.5	30																												
3.	Original Model Maximize: $P=x_1-x_2+3x_3$ Subject To: $X_1+x_2 \leq 20$ $X_1+x_3=5$ $X_2+x_3 \geq 10$ $X_1, x_2, x_3 \geq 0$ Modified Problem Maximize: $P=x_1-x_2+3x_3-Ma_1-Ma_2$ Subject To: $X_1+x_2+s_1=20$ $X_1+x_3+a_1=5$ $X_2+x_3-s_2+a_2=10$ $X_1, x_2, x_3, s_1, s_2, a_1, a_2 \geq 0$ Solve using BigM method.	choice Q-4		15Marks	CO1																										
4.	A new airline has determined to enroll in the market. It is thinking about supplying flights out of Phoenix, AZ, and would initially like to travel to a three distinct locations: San Diego, San Francisco, and Las Vegas. The distances of every roundtrip flight going out of Phoenix are (approximately): 720 miles, 1500 miles, and 1140 miles, respectively. The enterprise would like to use the slogan, "the average price per flight is by no means more than \$200." As for costs, it anticipates flights to San Diego will run about 10% of airfare. Similarly, San Francisco will run 12% and Las Vegas will run 14% of airfare. The agency wishes to make certain that the overall average fee isn't any more than 10% of earned airfare. Recent marketplace research permits the business enterprise to finish that it is able to probably promote about 1900 San Diego tickets, 700 San Francisco tickets, and 1000 Las Vegas ticket. Under these conditions and assuming that all tickets offered are round-experience flights, how much ought to the employer charge consistent with ticket that allows you to maximize its overall revenue? Solve the problem simplex method.			15Marks	CO1																										
5.	Differentiate Primal and Dual in linear programming. Give an example for how to convert from Primal to Dual.	choice Q-6		10Marks	CO2																										
6.	An individual on a high protein, low carbohydrate diet requires at least 100 units of protein and most 24 units of carbohydrates daily. The diet will consist entirely of three special liquid diet foods, A, B and C. The contents and costs of the diet foods are given below. How many bottles of each brand of diet food should be consumed daily in order to meet the protein and carbohydrate requirements at minimum cost? What is the minimum cost? Find the solution using dual method.			10Marks	CO2																										
7.	A enterprise manufactures two products X and Y on 3 machines Turning, Milling and finishing machines. Each unit of X takes, 10 hours of turning device capacity, five hours of milling machine potential and 1 hour of finishing system potential. One unit of Y takes 6 hours of turning machine ability, 10 hours of milling gadget capacity and 2 hours of finishing machine capability. The organization has 2500 hours of turning gadget capability, 2000 hours of milling device capability and 500 hours of completing gadget ability in the coming planning period. The income contribution of product X and Y are Rs. 23 in keeping with unit and Rs. 32 per unit respectively. Formulate the linear programming problem for Primal and Dual.	choice Q-8		15Marks	CO2																										
8.	The physician advises a patient visited him that the patient is weak in his health due to scarcity of two vitamins, ie, vitamin X and vitamin Y. He advises him to take as minimum 40 units of diet X and 50 units of Vitamin Y every day. He additionally advises that these vitamins are to be had in two tonics A and B. Each unit of tonic A includes 2 units of nutrition X and 3 gadgets of vitamin Y. Each unit of tonic B consists of 4 units of diet X and 2 units of nutrition Y. Tonic A and B are available inside the medical shop at a price of Rs. three in step with unit of A and Rs. 2,50 in line with unit of B. The patient has to meet the want of nutrition by ingesting A and B at a minimum fee. Mention whose problem is Primal and Dual. Formulate accordingly and give the solution for Primal and Dual.			15Marks	CO2																										
9.	Four different jobs are to be done on four different machines. The setup and production times are prohibitively high for changeover. The following table indicates the cost of producing job I on machine j in rupees. Assign jobs to different machines so that total cost is minimized.	choice Q-10		10Marks	CO3																										

Jobs	Machines			
	1	2	3	4
J1	5	7	11	6
J2	8	5	9	6
J3	4	7	10	7
J4	10	4	8	3

10.	Explain the following in context of Transportation Problem: a) Stepping Stone Method b) Modified Distribution Method		10Marks	CO3
-----	--	--	---------	-----

11.	<p>A manufacturer of electronic calculators produces its goods in Dallas, Chicago, and Boston, and maintains regional warehousing distribution centers in Philadelphia, Atlanta, Cleveland, and Washington, D.C. The company's staff has determined that shipping costs are directly proportional to the distances from factory to storage center, as listed here. a) Use the Column minimum method to arrive at an initial feasible solution. b) Show that the feasible solution determined in (a) is optimal.</p> <table border="1"> <thead> <tr> <th>Mileage/Warehouses</th> <th>Philadelphia</th> <th>Atlanta</th> <th>Cleveland</th> <th>Washington</th> </tr> </thead> <tbody> <tr> <td>Boston</td> <td>300</td> <td>1000</td> <td>500</td> <td>400</td> </tr> <tr> <td>Chicago</td> <td>500</td> <td>900</td> <td>300</td> <td>600</td> </tr> <tr> <td>Dallas</td> <td>1300</td> <td>1000</td> <td>1100</td> <td>1200</td> </tr> </tbody> </table> <p>The cost per calculator-mile is \$0.0002 and supplies and demands are:</p> <table border="1"> <thead> <tr> <th>Supply</th> <th>Demand</th> </tr> </thead> <tbody> <tr> <td>Boston 1500</td> <td>Philadelphia 2000</td> </tr> <tr> <td>Chicago 2500</td> <td>Atlanta 1600</td> </tr> <tr> <td>Dallas 4000</td> <td>Cleveland 1200</td> </tr> <tr> <td></td> <td>Washington 3200</td> </tr> </tbody> </table>	Mileage/Warehouses	Philadelphia	Atlanta	Cleveland	Washington	Boston	300	1000	500	400	Chicago	500	900	300	600	Dallas	1300	1000	1100	1200	Supply	Demand	Boston 1500	Philadelphia 2000	Chicago 2500	Atlanta 1600	Dallas 4000	Cleveland 1200		Washington 3200	choice Q-12	15Marks	CO3
Mileage/Warehouses	Philadelphia	Atlanta	Cleveland	Washington																														
Boston	300	1000	500	400																														
Chicago	500	900	300	600																														
Dallas	1300	1000	1100	1200																														
Supply	Demand																																	
Boston 1500	Philadelphia 2000																																	
Chicago 2500	Atlanta 1600																																	
Dallas 4000	Cleveland 1200																																	
	Washington 3200																																	

12.	<p>The Indiana tobacco company purchases tobacco and stores in warehouses located in the following four cities:</p> <table border="1"> <thead> <tr> <th>Warehouse</th> <th>Capacity(Tons)</th> </tr> </thead> <tbody> <tr> <td>Delhi</td> <td>90</td> </tr> <tr> <td>Kolkata</td> <td>50</td> </tr> <tr> <td>Ahmadabad</td> <td>80</td> </tr> <tr> <td>Chennai</td> <td>60</td> </tr> </tbody> </table> <p>The warehouse supply tobacco to cigarette companies situated at three cities that have the following demand:</p> <table border="1"> <thead> <tr> <th>Cigarette company</th> <th>Demand(tons)</th> </tr> </thead> <tbody> <tr> <td>Bharat</td> <td>120</td> </tr> <tr> <td>Janata</td> <td>100</td> </tr> <tr> <td>Red Lamp</td> <td>110</td> </tr> </tbody> </table> <p>The railroad shipping cost per ton are given below:</p> <table border="1"> <thead> <tr> <th>From/To</th> <th>Bharat</th> <th>Janata</th> <th>Red lamp</th> </tr> </thead> <tbody> <tr> <td>Delhi</td> <td>7</td> <td>10</td> <td>5</td> </tr> <tr> <td>Kolkata</td> <td>12</td> <td>9</td> <td>4</td> </tr> <tr> <td>Ahmadabad</td> <td>7</td> <td>3</td> <td>11</td> </tr> <tr> <td>Chennai</td> <td>9</td> <td>5</td> <td>7</td> </tr> </tbody> </table> <p>Because of railroad construction, shipments are temporarily prohibited from Warehouse at Delhi to Bharat Cigarette company. Find the optimal distribution cost for Indiana tobacco company.</p>	Warehouse	Capacity(Tons)	Delhi	90	Kolkata	50	Ahmadabad	80	Chennai	60	Cigarette company	Demand(tons)	Bharat	120	Janata	100	Red Lamp	110	From/To	Bharat	Janata	Red lamp	Delhi	7	10	5	Kolkata	12	9	4	Ahmadabad	7	3	11	Chennai	9	5	7		15Marks	CO3
Warehouse	Capacity(Tons)																																									
Delhi	90																																									
Kolkata	50																																									
Ahmadabad	80																																									
Chennai	60																																									
Cigarette company	Demand(tons)																																									
Bharat	120																																									
Janata	100																																									
Red Lamp	110																																									
From/To	Bharat	Janata	Red lamp																																							
Delhi	7	10	5																																							
Kolkata	12	9	4																																							
Ahmadabad	7	3	11																																							
Chennai	9	5	7																																							

13.	<p>The following knapsack problem: Maximize $\sum_{j=1}^n c_j x_j$, subject to: $\sum_{j=1}^n 2x_j \leq n$, $x_j = 0$ or 1 ($j = 1, 2, \dots, n$), Which has the same "contribution" for each item under consideration, has proved to be rather difficult to solve for most general purpose integer-programming codes when n is an odd number. a) What is the optimal solution when n is even? When n is odd? b) Comment specifically on why this problem might be difficult to solve on general integer-programming codes when n is odd.</p>	choice Q-14	10Marks	CO4
-----	--	-------------	---------	-----

14.	What is integer linear programming? Explain the merits and demerits of "rounding-off" a continuous optimal solution to an LP problem in order to obtain an integer solution.		10Marks	CO4
-----	--	--	---------	-----

15.	Consider the capital budgeting problem where five projects are being considered for execution over the next 3 years. The expected returns for each project and the yearly expenditures (in thousands of rupees) are shown in table. Assume that each approved project will be executed over the 3 year period. The objective is to select a combination of projects that will maximize the total returns. Formulate but not solve the mathematical programming problem.	choice Q-16	15Marks	CO4
-----	---	-------------	---------	-----

Expenditure for				
Project	Year 1	Year 2	Year 3	Returns
1	5	1	8	20
2	4	7	10	40
3	3	9	2	20
4	7	4	1	15
5	8	6	10	30
Maximum available funds	25	25	25	

16.	Solve the following linear programming problem using Branch and Bound Method: Maximize $Z=3x_1+2x_2$ Subject to $2x_1+5x_2 \leq 9$ $4x_1+2x_2 \leq 9$ $x_1, x_2 \geq 0$ and integers			15Marks	CO4
-----	--	--	--	---------	-----

[object HTMLDivElement]